

**1E3101**

Roll No.

Total No. of Pages. ☐**1E3101****B. Tech. I - Sem. (Main / Back) Exam., - 2025****1FY2-01 Engineering Mathematics - I****Time: 3 Hours****Maximum Marks: 70***Instructions to Candidates:*

*Attempt all ten questions from Part A, five questions out of seven questions from Part B and three questions out of five from Part C.*

*Schematic diagrams must be shown wherever necessary. Any data you feel missing may suitably be assumed and stated clearly. Units of quantities used /calculated must be stated clearly.*

*Use of following supporting material is permitted during examination.  
(Mentioned in form No. 205)*

1. NIL2. NIL**PART - A****[10×2=20]****(Answer should be given up to 25 words only)****All questions are compulsory**Q.1 Evaluate -  $\int_0^1 x^2(1-x)^3 dx$ Q.2 Test the convergence of  $\int_1^{\infty} \frac{dx}{x^{3/2}}$ .

Q.3 What is Convergence and Divergence of a sequence?

Q.4 Find the interval of convergence of Exponential and Logarithmic series.

Q.5 Write Euler's formula of Fourier Series.

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Q.6 Find half range sine series for the function  $f(x) = x$  in the interval  $0 < x < z$ .

Q.7 If  $u = e^{xyz}$ , then find  $\frac{\partial^3 u}{\partial x \partial y \partial z}$ .

Q.8 Write the equation of the tangent plane to the surface  $z = f(x, y)$ .

Q.9 Change the order of integration and then evaluate -  $\int_0^1 \int_{x^2}^{2-x} xy \, dx \, dy$ .

Q.10 Write the statement of Green theorem.

### **PART – B**

[5×4=20]

#### **(Analytical/Problem solving questions)**

#### **Attempt any five questions**

Q.1 Show that  $\int_0^\infty \frac{x^2 \, dx}{(1+x^4)^3} = \frac{5\pi\sqrt{2}}{128}$ . <https://www.rtuonline.com>

Q.2 Test for convergence of the series  $\sum \frac{1}{\sqrt{n} + \sqrt{n+1}}$ .

Q.3 Find the Fourier series to represent  $f(x) = |x|$  for  $-\pi < x < \pi$ .

Q.4 Find the directional derivative of  $\phi = x^2 - 2y^2 + 4z^2$  at  $(1, 1, -1)$  in the direction of the vector  $2\hat{i} + \hat{j} - \hat{k}$ . Also find the direction of maximum directional derivative at  $(1, 1, -1)$  and its max value.

Q.5 Find the limit and test for continuity of the function

$$f(x, y) = \begin{cases} \frac{x^3 - y^3}{x + y} & \text{if } x + y \neq 0 \\ 0 & \text{if } x + y = 0 \end{cases} \text{ at the point } (0, 0).$$

Q.6 Evaluate  $\iint_R (x^2 + y^2) \, dx \, dy$  where  $R$  is the region bounded by  $y = x$  and  $y^2 = 4x$ .

Q.7 Evaluate  $\iiint_V f \, dV$  where  $f = 2x + y$ ,  $V$  is the closed region bounded by the cylinder  $z = 4 - x^2$  and the plane  $x = y = z = 0$  and  $y = z$ .

## **PART – C**

[3×10=30]

**(Descriptive/Analytical/Problem Solving/Design Questions)**

**Attempt any three questions**

- Q.1 Find the Fourier Series to represent  $f(x) = x - x^2$  in the interval  $-1 < x < 1$ .
- Q.2 Test the convergence of the series  $\frac{1^2}{2^2} + \frac{1^2 \cdot 3^2}{2^2 \cdot 4^2} + \frac{1^2 \cdot 3^2 \cdot 5^2}{2^2 \cdot 4^2 \cdot 6^2} + \dots$
- Q.3 If  $u = f(r)$ ,  $r^2 = x^2 + y^2$  show that  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f''(r) + \frac{1}{r} f'(r)$ .
- Q.4 Find the volume of greatest rectangular parallelepiped inscribed in the ellipsoid whose equation is  $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ .
- Q.5 Verify Stokes theorem for  $F = (x^2 + y - 4)\hat{i} + 3xy\hat{j} + (2xz + z^2)\hat{k}$  over the surface of the hemisphere  $x^2 + y^2 + z^2 = 16$  above the  $xy$  plane.
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